

$$\text{ELP}_{\chi_0, \chi_3}(\mathbf{C}) \geq \prod_{i=1}^3 \text{ELP}_{\chi_{i-1}, \chi_i}(\mathbf{R}_i)$$