Quantitative Security of Block Ciphers: Designs and Cryptanalysis Tools

Thomas Baignères



PhD Defense September 26, 2008

Prologue

A Typical Iterated Block Cipher

• A block cipher on a finite set is a family of permutations on that set, indexed by a parameter call the key.



A Typical Iterated Block Cipher

- A block cipher on a finite set is a family of permutations on that set, indexed by a parameter call the key.
- Such a cipher is usually iterated, i.e., made of several rounds.
- Each round is parameterized by a key derived from the main secret key by means of a Key Schedule.



A Typical Iterated Block Cipher

- A block cipher on a finite set is a family of permutations on that set, indexed by a parameter call the key.
- Such a cipher is usually iterated, i.e., made of several rounds.
- Each round is parameterized by a key derived from the main secret key by means of a Key Schedule.
- Usually, the rounds all share the same design, e.g., a round key addition followed by a fixed (nonlinear) transformation.











Motivation

"[...] the methodology of provable security has become unavoidable in designing and evaluating new schemes" [JSe03]

Motivation

"[...] the methodology of provable security has become unavoidable in designing and evaluating new schemes" [JSe03]

We will provide tools to evaluate and design new schemes!

Part I: On the (In)Security of Block Ciphers: Tools for the Security Analysis

Distinguishers between two sources

Projection-based distinguishers between two sources



Distinguishers between two sources

Projection-based distinguishers between two sources

- The game: distinguishing between two sources of randomness
- The optimal solution
- Complexity analysis: How many samples do we need to distinguish with a given efficiency?

Distinguishers between two sources

Projection-based distinguishers between two sources

- What if the optimal solution cannot be implemented?
- Distinguishing in practice using compression
- Example: Generalized linear distinguisher

Distinguishers between two sources

Projection-based distinguishers between two sources

- From random sources to random permutations
- A toolbox for generalized linear cryptanalysis of block ciphers
- Cryptanalysis of SAFER K/SK
- DEAN

Distinguishers between two sources

Projection-based distinguishers between two sources

Practical Implications for block ciphers

- From random sources to random permutations
- A toolbox for generalized linear cryptanalysis of block ciphers
- Cryptanalysis of SAFER K/SK
- DEAN

[BJVa04] [BSVsac07] [BVicits08]

Part I: On the (In)Security of Block Ciphers: Tools for the Security Analysis Distinguisher between two Sources

• P_0 and P_1 are two arbitrary distributions over a finite set Z.

• P_0 and P_1 are two arbitrary distributions over a finite set Z.



• P_0 and P_1 are two arbitrary distributions over a finite set Z.



- S generates q samples $\sim \mathsf{P}_0$ or P_1
- \mathcal{A} outputs 1 iff it guesses that P_1 is the the correct distribution

• P_0 and P_1 are two arbitrary distributions over a finite set Z.



- S generates q samples $\sim \mathsf{P}_0$ or P_1
- \mathcal{A} outputs 1 iff it guesses that P_1 is the the correct distribution
- The ability of A to distinguish P_0 from P_1 is its advantage:

 $\operatorname{Adv}_{\mathcal{A}}(\mathsf{P}_0,\mathsf{P}_1) = |\operatorname{Pr}_{\mathsf{P}_0}[\mathcal{A}(Z_1,\ldots,Z_q) = 1] - \operatorname{Pr}_{\mathsf{P}_1}[\mathcal{A}(Z_1,\ldots,Z_q) = 1]|$

- *A* is computationally unbounded (deterministic)
- *q* samples are independent (order is irrelevant)
- What matters: the number of occurrences of each symbol of \mathcal{Z} in the string Z_1, \ldots, Z_q
- Equivalently: the type $P_{Z_1,...,Z_q}$ of the sequence:

$$\mathsf{P}_{Z_1,...,Z_q}[a] = \frac{\#\{i \, : \, Z_i = a\}}{q}$$

- A is computationally unbounded (deterministic)
- *q* samples are independent (order is irrelevant)
- What matters: the number of occurrences of each symbol of \mathcal{Z} in the string Z_1, \ldots, Z_q
- Equivalently: the type $P_{Z_1,...,Z_q}$ of the sequence:

$$\mathsf{P}_{Z_1,...,Z_q}[a] = \frac{\#\{i \, : \, Z_i = a\}}{q}$$

• Example: $\mathcal{Z} = \{1, 2, 3\}$, q = 13 and $Z_1, Z_2, \dots, Z_{13} = 1322312313221$

$$\mathsf{P}_{Z_1,\dots,Z_{13}}[\mathbf{1}] = \frac{4}{13} \qquad \qquad \mathsf{P}_{Z_1,\dots,Z_{13}}[\mathbf{2}] = \frac{5}{13} \qquad \qquad \mathsf{P}_{Z_1,\dots,Z_{13}}[\mathbf{3}] = \frac{4}{13}$$

 \mathcal{A} uniquely determined by Π_q :

$$\mathsf{P}_{Z_1,\ldots,Z_q} \in \Pi_q \iff \mathcal{A}(Z_1,\ldots,Z_q) = 1$$

 \mathcal{A} uniquely determined by Π_q :

$$\mathsf{P}_{Z_1,\ldots,Z_q} \in \Pi_q \iff \mathcal{A}(Z_1,\ldots,Z_q) = 1$$

Number of such Π_q is finite \square Number of possible adversaries is finite.

 \mathcal{A} uniquely determined by Π_q :

$$\mathsf{P}_{Z_1,\ldots,Z_q} \in \Pi_q \iff \mathcal{A}(Z_1,\ldots,Z_q) = 1$$

Number of such Π_q is finite \square Number of possible adversaries is finite.

An optimal distinguisher exists!



Using maximum-likelihood techniques, the *q*-limited distinguisher \mathcal{A}^* defined by

$$\Pi^{\star} = \{ \mathsf{P} \ : \ \mathrm{D}(\mathsf{P} \| \mathsf{P}_{1}) - \mathrm{D}(\mathsf{P} \| \mathsf{P}_{0}) \le 0 \}$$

can be shown to be optimal.

Using maximum-likelihood techniques, the *q*-limited distinguisher \mathcal{A}^* defined by

$$\Pi^{\star} = \{ \mathsf{P} \ : \ \mathrm{D}(\mathsf{P} \| \mathsf{P}_1) - \mathrm{D}(\mathsf{P} \| \mathsf{P}_0) \le 0 \}$$

can be shown to be optimal.

$$D(p||q) = \sum_{a \in \mathcal{Z}} p[a] \log \frac{p[a]}{q[a]}$$
 always non-negative, 0 iff $p=q$, infinite iff $Supp(p) \not\subseteq Supp(q)$

Using the theory of types & Sanov's theorem

asymptotic data complexity of \mathcal{A}^* .

Using the theory of types & Sanov's theorem \implies asymptotic data complexity of \mathcal{A}^* .

Using the theory of types & Sanov's theorem \implies asymptotic data complexity of \mathcal{A}^* .

Theorem

Let P_0 and P_1 be two distributions s.t. $Supp(P_0) \cup Supp(P_1) = Z$. The advantage of \mathcal{A}^* verifies

$$1 - \text{BestAdv}_q(\mathsf{P}_0, \mathsf{P}_1) \doteq 2^{-q\mathsf{C}(\mathsf{P}_0, \mathsf{P}_1)}$$

where

$$C(\mathsf{P}_0,\mathsf{P}_1) = -\inf_{0<\lambda<1}\log\sum_{a\in\mathsf{Supp}(\mathsf{P}_0)\cap\mathsf{Supp}(\mathsf{P}_1)}\mathsf{P}_0[a]^{1-\lambda}\mathsf{P}_1[a]^{\lambda}$$

is the Chernoff information between P_0 and P_1 .

Using the theory of types & Sanov's theorem \implies asymptotic data complexity of \mathcal{A}^* .

Theorem

Let P_0 and P_1 be two distributions s.t. $Supp(P_0) \cup Supp(P_1) = Z$. The advantage of \mathcal{A}^* verifies

$$1 - \text{BestAdv}_q(\mathsf{P}_0, \mathsf{P}_1) \doteq 2^{-q\mathsf{C}(\mathsf{P}_0, \mathsf{P}_1)}$$

where

$$C(\mathsf{P}_0,\mathsf{P}_1) = -\inf_{0<\lambda<1}\log\sum_{a\in\mathsf{Supp}(\mathsf{P}_0)\cap\mathsf{Supp}(\mathsf{P}_1)}\mathsf{P}_0[a]^{1-\lambda}\mathsf{P}_1[a]^{\lambda}$$

is the Chernoff information between $\mathsf{P}_0\,$ and P_1 .

Notation: $f(q) \doteq g(q)$ means that $f(q) = g(q)e^{o(q)}$, i.e., $\lim_{q \to \infty} \frac{1}{q} \log \frac{f(q)}{g(q)} = 0$.

Thomas Baignères

Using the theory of types & Sanov's theorem \implies asymptotic data complexity of \mathcal{A}^* .

Theorem

Let P_0 and P_1 be two distributions s.t. $Supp(P_0) \cup Supp(P_1) = Z$. The advantage of \mathcal{A}^* verifies

$$1 - \text{BestAdv}_q(\mathsf{P}_0, \mathsf{P}_1) \doteq 2^{-q\mathrm{C}(\mathsf{P}_0, \mathsf{P}_1)}$$

where

$$\mathcal{C}(\mathsf{P}_0,\mathsf{P}_1) \approx \frac{\|\mathsf{P}_1 - \mathsf{P}_0\|_2^2}{8\ln 2}$$

is the Chernoff information between P_0 and P_1 .

Notation: $f(q) \doteq g(q)$ means that $f(q) = g(q)e^{o(q)}$, i.e., $\lim_{q \to \infty} \frac{1}{q} \log \frac{f(q)}{g(q)} = 0$.

Thomas Baignères

Using the theory of types & Sanov's theorem \implies asymptotic data complexity of \mathcal{A}^* .

Theorem

Let P_0 and P_1 be two distributions s.t. $Supp(P_0) \cup Supp(P_1) = Z$. The advantage of \mathcal{A}^* verifies

$$1 - \text{BestAdv}_q(\mathsf{P}_0, \mathsf{P}_1) \approx 2^{-q\mathrm{C}(\mathsf{P}_0, \mathsf{P}_1)}$$

where

$$C(P_0, P_1) \approx \frac{\|P_1 - P_0\|_2^2}{8\ln 2}$$

is the Chernoff information between P_0 and P_1 .

Using the theory of types & Sanov's theorem \blacksquare asymptotic data complexity of \mathcal{A}^* .




$$\mathsf{P}_0 = (\frac{1}{2}, \frac{1}{2})$$
 $\mathsf{P}_1 = (\frac{1}{2}(1-\epsilon), \frac{1}{2}(1+\epsilon))$

$$C(\mathsf{P}_0,\mathsf{P}_1) = -\inf_{0<\lambda<1}\log\frac{1}{2}\left((1-\epsilon)^{\lambda} + (1+\epsilon)^{\lambda}\right)$$



$$P_{0} = \left(\frac{1}{2}, \frac{1}{2}\right) \qquad P_{1} = \left(\frac{1}{2}(1-\epsilon), \frac{1}{2}(1+\epsilon)\right)$$

$$C(P_{0}, P_{1}) = -\inf_{0 < \lambda < 1} \log \frac{1}{2} \left((1-\epsilon)^{\lambda} + (1+\epsilon)^{\lambda}\right)$$
Minimum reached for $\lambda \approx \frac{1}{2}$

$$C(P_{0}, P_{1}) \approx -\log \left(1 - \frac{\epsilon^{2}}{8}\right) \approx \frac{\epsilon^{2}}{8 \ln 2}$$

$$Example with \epsilon = 0.01$$



Approximating $1 - \text{BestAdv}_q(P_0, P_1)$ by its asymptotic value, we deduce that

$$q \approx \frac{8\ln 2}{\epsilon^2}$$

allow to reach a non-negligible advantage.

Thomas Baignères

 $\mathsf{P}_0 = \left(\frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}\right) \qquad \mathsf{P}_1 = \left(\frac{1}{6}, \frac{1}{6}, \frac{2}{6}, 0, \frac{1}{6}, \frac{1}{6}\right)$

 $\mathsf{P}_0 = \left(\frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{1}{6}\right) \qquad \mathsf{P}_1 = \left(\frac{1}{6}, \frac{1}{6}, \frac{2}{6}, 0, \frac{1}{6}, \frac{1}{6}\right)$

$$C(\mathsf{P}_0,\mathsf{P}_1) = \max_{0 < \lambda < 1} \log\left(\frac{6}{2^{\lambda} + 4}\right)$$





 $1 - \text{BestAdv}_q(\mathsf{P}_0, \mathsf{P}_1) \doteq 2^{-0.263 \cdot q}$



$$1 - \text{BestAdv}_q(\mathsf{P}_0, \mathsf{P}_1) \doteq 2^{-0.263 \cdot q}$$

+This is the proof that all this theory has a practical application...

- Case where the distributions are "close" to each other
- Case where one of the hypotheses is composite
- Case where one of the two distributions is unknown
- etc.

Part I: On the (In)Security of Block Ciphers: Tools for the Security Analysis Projection Based Distinguishers

On the Need for Projection-Based Distinguishers

• If $|\mathcal{Z}|$ is too large, the best distinguisher cannot be implemented.

On the Need for Projection-Based Distinguishers

- If $|\mathcal{Z}|$ is too large, the best distinguisher cannot be implemented.
- Possible solution: reduce the sample size using a projection:



- $\mathcal{Z} = \{0,1\}^n$ $\mathcal{G} = \{0,1\}$ $\mathsf{P}_0 = \mathsf{U}$ $\mathsf{P}_1 = \mathsf{P}$ $h(Z) = a \cdot Z = a_1 Z_1 \oplus \cdots \oplus a_n Z_n$
- This is a linear distinguisher based on the mask *a*.

- $\mathcal{Z} = \{0,1\}^n$ $\mathcal{G} = \{0,1\}$ $\mathsf{P}_0 = \mathsf{U}$ $\mathsf{P}_1 = \mathsf{P}$ $h(Z) = a \cdot Z = a_1 Z_1 \oplus \cdots \oplus a_n Z_n$
- This is a linear distinguisher based on the mask *a*.
- By implementing the optimal strategy (after the linear compression), the advantage of this linear distinguisher verifies:

 $1 - \operatorname{Adv}(\mathsf{U},\mathsf{P}) \doteq 2^{-q\operatorname{C}(\overline{\mathsf{U}},\overline{\mathsf{P}})}$

- $\mathcal{Z} = \{0,1\}^n$ $\mathcal{G} = \{0,1\}$ $\mathsf{P}_0 = \mathsf{U}$ $\mathsf{P}_1 = \mathsf{P}$ $h(Z) = a \cdot Z = a_1 Z_1 \oplus \cdots \oplus a_n Z_n$
- This is a linear distinguisher based on the mask *a*.
- By implementing the optimal strategy (after the linear compression), the advantage of this linear distinguisher verifies:



- $\mathcal{Z} = \{0,1\}^n$ $\mathcal{G} = \{0,1\}$ $\mathsf{P}_0 = \mathsf{U}$ $\mathsf{P}_1 = \mathsf{P}$ $h(Z) = a \cdot Z = a_1 Z_1 \oplus \cdots \oplus a_n Z_n$
- This is a linear distinguisher based on the mask *a*.
- By implementing the optimal strategy (after the linear compression), the advantage of this linear distinguisher verifies:



- $\mathcal{Z} = \{0,1\}^n$ $\mathcal{G} = \{0,1\}$ $\mathsf{P}_0 = \mathsf{U}$ $\mathsf{P}_1 = \mathsf{P}$ $h(Z) = a \cdot Z = a_1 Z_1 \oplus \cdots \oplus a_n Z_n$
- This is a linear distinguisher based on the mask *a*.
- By implementing the optimal strategy (after the linear compression), the advantage of this linear distinguisher verifies:



- The previous example only works for sets of the form $\mathcal{Z} = \{0, 1\}^n$.
- We at least need to generalize the notion of linear probability to arbitrary sets.

- The previous example only works for sets of the form $\mathcal{Z} = \{0, 1\}^n$.
- We at least need to generalize the notion of linear probability to arbitrary sets.

The linear probability of P over the group $\mathcal Z$ with respect to the character χ is

 $LP_{\chi}(\mathsf{P}) = |E_{\mathsf{P}}(\chi(Z))|^2$

Definition

- The previous example only works for sets of the form $\mathcal{Z} = \{0, 1\}^n$.
- We at least need to generalize the notion of linear probability to arbitrary sets.

Definition The linear probability of P over the group \mathcal{Z} with respect to the character χ is $LP_{\chi}(P) = |E_{P}(\chi(Z))|^{2}$

- A character of \mathcal{Z} is a homomorphism $\chi : \mathcal{Z} \longrightarrow \mathbf{C}^{\times}$
- Example: when $\mathcal{Z} = \{0,1\}^n$ we have $\chi(a) = (-1)^{u \cdot a}$ for some u

- The previous example only works for sets of the form $\mathcal{Z} = \{0, 1\}^n$.
- We at least need to generalize the notion of linear probability to arbitrary sets.

Definition

The linear probability of P over the group \mathcal{Z} with respect to the character χ is

 $LP_{\chi}(\mathsf{P}) = |E_{\mathsf{P}}(\chi(Z))|^2$

- A character of \mathcal{Z} is a homomorphism $\chi : \mathcal{Z} \longrightarrow \mathbf{C}^{\times}$
- Example: when $\mathcal{Z} = \{0,1\}^n$ we have $\chi(a) = (-1)^{u \cdot a}$ for some u
- Consequence: when $\mathcal{Z} = \{0,1\}^n$ this new definition corresponds to the old one!

Lin. Distinguishers for Sources overs Arbitrary Sets

We have wonderful lemma...

We have wonderful lemma...

Lemma 7.5 Let P_0 be the uniform distribution on a finite subgroup H of C^{\times} of order d. Let $\mathcal{D} = \{P_u : u \in H\}$ be a set of d distributions on H defined by (7.10). The q-limited distinguisher between the null hypothesis $H_0 : P = P_0$ and the alternate hypothesis $H_1 : P \in \mathcal{D}$ defined by the distribution acceptance region $\Pi_q^{\star} = \Pi^{\star} \cap \mathcal{P}_q$, where

$$\Pi^{\star} = \left\{ \mathsf{P} \in \mathcal{P} : \|\mathsf{P}\|_{\infty} \ge \frac{\log(1-\epsilon)}{\log(1-\epsilon) - \log(1+(d-1)\epsilon)} \right\},\tag{7.11}$$

is asymptotically optimal and its advantage $BestAdv_q$ is such that

1 - BestAdv_q(H₀, H₁)
$$\doteq 2^{q \inf_{0 < \lambda < 1} \log \frac{1}{d} \left((1 + (d-1)\epsilon)^{\lambda} + (d-1)(1-\epsilon)^{\lambda} \right)}.$$

Lin. Distinguishers for Sources overs Arbitrary Sets

We have wonderful lemma...



Part I: On the (In)Security of Block Ciphers: Tools for the Security Analysis Practical Implications for Block Ciphers

Distinguishing Random Permutations

- A simple trick allows to turn distinguishers of random sources into distinguishers of random permutations (block ciphers).
- All the results on random sources apply to random permutations.
- In the case of the generalization of linear cryptanalysis:

$$LP_{\rho,\mu}(\mathsf{C}_k) = \left| E_{P \in \mathsf{UT}} \left(\overline{\rho}(P) \mu\left(\mathsf{C}_k(P)\right) \right) \right|^2$$



Distinguishing Random Permutations

- A simple trick allows to turn distinguishers of random sources into distinguishers of random permutations (block ciphers).
- All the results on random sources apply to random permutations.
- In the case of the generalization of linear cryptanalysis:

$$LP_{\rho,\mu}(\mathsf{C}_k) = \left| E_{P \in \mathsf{UT}} \left(\overline{\rho}(P) \mu\left(\mathsf{C}_k(P)\right) \right) \right|^2$$



• $\operatorname{ELP}_{\rho,\mu}(\mathsf{C}) = \operatorname{E}_{K}(\operatorname{LP}_{\rho,\mu}(\mathsf{C}_{K}))$

• Apply a bottom-up approach



- Apply a bottom-up approach
- We provide a toolbox that allows, for any given output character, to find the input characters that maximizes the ELP over various building blocks.



- Apply a bottom-up approach
- We provide a toolbox that allows, for any given output character, to find the input characters that maximizes the ELP over various building blocks.
- Easy to deduce a ELP over one round



- Apply a bottom-up approach
- We provide a toolbox that allows, for any given output character, to find the input characters that maximizes the ELP over various building blocks.
- Easy to deduce a ELP over one round
- For a Markov cipher C = R₃ o R₂ o R₁, we show that Nyberg's linear hull effect applies:

$$\operatorname{ELP}_{\chi_0,\chi_3}(\mathsf{C}) = \sum_{\chi_1,\chi_2} \prod_{i=1}^3 \operatorname{ELP}_{\chi_{i-1},\chi_i}(\mathsf{R}_i)$$



- Apply a bottom-up approach
- We provide a toolbox that allows, for any given output character, to find the input characters that maximizes the ELP over various building blocks.
- Easy to deduce a ELP over one round
- For a Markov cipher C = R₃ o R₂ o R₁, we show that Nyberg's linear hull effect applies:

$$\operatorname{ELP}_{\chi_0,\chi_3}(\mathsf{C}) = \sum_{\chi_1,\chi_2} \prod_{i=1}^3 \operatorname{ELP}_{\chi_{i-1},\chi_i}(\mathsf{R}_i)$$

• Use the last property to pile ELP's up: $ELP_{\chi_0,\chi_3}(\mathsf{C}) \ge \prod_{i=1}^{3} ELP_{\chi_{i-1},\chi_i}(\mathsf{R}_i)$

Applications on SAFER K/SK

- We attack SAFER with a ⊞-linear cryptanalysis.
- Use the toolbox to find characteristics within SAFER K/SK.
- To compute the complexities we consider several characteristics among the hull (i.e., all characteristics share the same input/output characters).
- To turn distinguishing attacks into key recovery attacks, we also take advantage of the linearity of the key schedule.

Applications on SAFER K/SK

- We attack SAFER with a ⊞-linear cryptanalysis.
- Use the toolbox to find characteristics within SAFER K/SK.
- To compute the complexities we consider several characteristics among the hull (i.e., all characteristics share the same input/output characters).
- To turn distinguishing attacks into key recovery attacks, we also take advantage of the linearity of the key schedule.

Nbr Rounds	Complexity
2	$2^{23}/2^{31}$
3	2^{38}
4	2^{49}
5	2^{56}

Other Applications

- Two new Digital Encryption Algorithm for Numbers (based on the AES): DEAN18 and DEAN27 which respectively encrypts blocks made of 18 and 27 decimal digits.
- Resistance against our generalization of linear cryptanalysis.
- New attacks on TOY100 (toy cipher that encrypts blocks of 32 decimal digits).
- Break 9 (10 ?) rounds out of 12.
Part II: Designs and Security Proofs

The Decorrelation Theory

Dial C for Cipher

KFC: the Krazy Feistel Cipher

The Decorrelation Theory

Dial C for Cipher

KFC: the Krazy Feistel Cipher

- The Luby-Rackoff Model
- The quantity to minimize: the advantage of an adversary \mathcal{A}
- Distribution matrix of a block cipher
- Link between the advantage of A and the distance between distribution matrices
- Basic properties and decorrelation modules

The Decorrelation Theory

Dial C for Cipher

KFC: the Krazy Feistel Cipher



The Decorrelation Theory

Dial C for Cipher

KFC: the Krazy Feistel Cipher



The Decorrelation Theory

Dial C for Cipher

KFC: the Krazy Feistel Cipher



- Independence of the round keys
- Couldn't we use the Vernam cipher instead?

The Decorrelation Theory

Dial C for Cipher

KFC: the Krazy Feistel Cipher



- Independence of the round keys
- Couldn't we use the Vernam cipher instead?

[BVsac05] [BFsac06] [BFa06]

Part II: Designs and Security Proofs The Decorrelation Theory

We consider a q-limited adversary A in the Luby-Rackoff Model:

- computationally unbounded
- limited to q queries to an oracle \mathcal{O} implementing either
 - a random instance C of the block cipher
 - a random instance C^{*} of the perfect cipher
- the objective of $\mathcal A$ being to guess which is the case.

We consider a q-limited adversary A in the Luby-Rackoff Model:



We consider a q-limited adversary A in the Luby-Rackoff Model:



 \checkmark The block cipher C is secure if the advantage of \mathcal{A} is negligible for all \mathcal{A} 's.

We consider a q-limited adversary A in the Luby-Rackoff Model:



 \mathcal{A} is non-adaptive if the q plaintexts are chosen "at once".

We consider a q-limited adversary A in the Luby-Rackoff Model:



 \mathcal{A} is adaptive if plaintext *i* depends on ciphertexts $1, \ldots, i-1$.

Computing $\operatorname{Adv}_{\mathcal{A}}(\mathsf{C},\mathsf{C}^{\star})$

- Computing the advantage is not a trivial task in general.
- Possible solution: use Vaudenay's Decorrelation Theory.

$$\max_{\mathcal{A}} \operatorname{Adv}_{\mathcal{A}}(\mathsf{C},\mathsf{C}^{\star}) = \frac{1}{2} \|[\mathsf{C}]^{q} - [\mathsf{C}^{\star}]^{q}\|$$

Computing $\operatorname{Adv}_{\mathcal{A}}(\mathsf{C},\mathsf{C}^{\star})$

- Computing the advantage is not a trivial task in general.
- Possible solution: use Vaudenay's Decorrelation Theory.

$$[C]^{q} = \underbrace{\left[\begin{array}{c} C \end{array}\right]^{q}}_{\left[\mathcal{M}\right]^{q}} \\ \mathbb{C} \right]^{q} = \underbrace{\left[\begin{array}{c} C \end{array}\right]^{q}}_{\left[\mathcal{M}\right]^{q}} \\ \mathbb{C} \end{array}\right]^{q} \\ \mathbb{C}$$

Example!

On the set $\mathcal{M}=\{1,2,3\}$, the distribution matrices of the perfect cipher C* look like this (at orders 1 and 2):

$$\begin{bmatrix} \mathbb{C}^{\star} \end{bmatrix}^{1} = \begin{bmatrix} 1/3 & 1/3 & 1/3 \\ 1/3 & 1/3 & 1/3 \\ 1/3 & 1/3 & 1/3 \\ 1/3 & 1/3 & 1/3 \end{bmatrix} \stackrel{(1)}{(2)}$$

	(1,1)	(1,2)	(1,3)	(2,1)	(2,2)	(2,3)	(3,1)	(3,2)	(3,3)	
	1/3	0	0	0	1/3	0	0	0	1/3	(1,1)
	0	1/6	1/6	1/6	0	1/6	1/6	1/6	0	(1,2)
	0	1/6	1/6	1/6	0	1/6	1/6	1/6	0	(1,3)
	0	1/6	1/6	1/6	0	1/6	1/6	1/6	0	(2,1)
$[C^{\star}]^2 =$	1/3	0	0	0	1/3	0	0	0	1/3	(2,2)
	0	1/6	1/6	1/6	0	1/6	1/6	1/6	0	(2,3)
	0	1/6	1/6	1/6	0	1/6	1/6	1/6	0	(3,1)
	0	1/6	1/6	1/6	0	1/6	1/6	1/6	0	(3,2)
	1/3	0	0	0	1/3	0	0	0	1/3	(3,3)

Adaptive vs. non-Adaptive Adversaries

• The norm used to compute the distance between two distribution matrices depends on the kind of adversary we consider.

• If A is adaptive:

$$\max_{\mathcal{A}_{a}} \operatorname{Adv}_{\mathcal{A}_{a}}(\mathsf{C},\mathsf{C}^{\star}) = \frac{1}{2} \|[\mathsf{C}]^{q} - [\mathsf{C}^{\star}]^{q}\|_{\mathsf{a}}$$

$$||M||_{a} = \max_{x_{1}} \sum_{y_{1}} \cdots \max_{x_{q}} \sum_{y_{q}} |M_{x,y}|$$

• If A is non-adaptive:

$$\underbrace{\max_{\mathcal{A}_{na}} \operatorname{Adv}_{\mathcal{A}_{na}}(\mathsf{C},\mathsf{C}^{\star}) = \frac{1}{2} \|[\mathsf{C}]^{q} - [\mathsf{C}^{\star}]^{q}\|_{\infty}}_{\|M\|_{\infty} = \max_{x_{1},\dots,x_{q}} \sum_{y_{1},\dots,y_{q}} |M_{x,y}|}$$

Thomas Baignères

Are we done then? Not Quite :-<



Are we done then? Not Quite :-<





Tricks for Computing $\operatorname{Adv}_{\mathcal{A}}(\mathsf{C},\mathsf{C}^{\star})$

To deal with the size of the distribution matrices:

 $\mathbf{I} [\mathsf{C}_2 \circ \mathsf{C}_1]^q = [\mathsf{C}_1]^q \times [\mathsf{C}_2]^q$



Tricks for Computing $\operatorname{Adv}_{\mathcal{A}}(\mathsf{C},\mathsf{C}^{\star})$

To deal with the size of the distribution matrices:

 $\oint [\mathsf{C}_2 \circ \mathsf{C}_1]^q = [\mathsf{C}_1]^q \times [\mathsf{C}_2]^q$



Take advantage of the symmetries of the block cipher in order to compute the distribution matrix of each round



If $a = (a_1, \ldots, a_\ell)$ is an array of *m*-bit strings, the support of a is the array of $\{0, 1\}^\ell$ with 0's at the position where the entry of *a* is zero and 1's elsewhere

Example:



The weight w(a) of a is the hamming weight of the support (3 in the example).



- Independent random permutations
- input: $a = (a_1, ..., a_\ell)$
- output: $b = (b_1, ..., b_\ell)$
- $M = 2^m$



• Independent random permutations

• input:
$$a = (a_1, ..., a_\ell)$$

• output:
$$b = (b_1, ..., b_\ell)$$

•
$$M = 2^m$$

For each substitution box:

$$\Pr[\mathsf{S}_i^{\star}(a_i) = b_i, \mathsf{S}_i^{\star}(a_i') = b_i'] = \begin{cases} \frac{1}{M} & \text{if } a_i = a_i' \text{ and } b_i = b_i', \\ \frac{1}{M(M-1)} & \text{if } a_i \neq a_i' \text{ and } b_i \neq b_i', \\ 0 & \text{otherwise.} \end{cases}$$



• Independent random permutations

• input:
$$a = (a_1, ..., a_\ell)$$

• output:
$$b = (b_1, ..., b_\ell)$$

•
$$M = 2^m$$

For each substitution box:

$$\Pr[\mathsf{S}_i^{\star}(a_i) = b_i, \mathsf{S}_i^{\star}(a_i') = b_i'] = \begin{cases} \frac{1}{M} & \text{if } a_i = a_i' \text{ and } b_i = b_i', \\ \frac{1}{M(M-1)} & \text{if } a_i \neq a_i' \text{ and } b_i \neq b_i', \\ 0 & \text{otherwise.} \end{cases}$$

$$\sum \Pr[\mathsf{S}_{i}^{\star}(a_{i}) = b_{i}, \mathsf{S}_{i}^{\star}(a_{i}') = b_{i}',] = \mathbf{1}_{\operatorname{supp}(a_{i} \oplus a_{i}') = \operatorname{supp}(b_{i} \oplus b_{i}')} M^{-1}(M-1)^{-w(a_{i} \oplus a_{i}')}$$



• Independent random permutations

• input:
$$a = (a_1, ..., a_\ell)$$

• output:
$$b = (b_1, ..., b_\ell)$$

• $M = 2^m$

By independence:

$$[\mathsf{S}]^2_{(a,a'),(b,b')} = \prod_{i=1}^{\ell} \Pr[\mathsf{S}^{\star}_i(a_i) = b_i, \mathsf{S}^{\star}_i(a'_i) = b'_i]$$



• Independent random permutations

• input:
$$a = (a_1, ..., a_\ell)$$

• output:
$$b = (b_1, ..., b_\ell)$$

• $M = 2^m$

By independence:

$$[\mathsf{S}]^2_{(a,a'),(b,b')} = \prod_{i=1}^{\ell} \Pr[\mathsf{S}^{\star}_i(a_i) = b_i, \mathsf{S}^{\star}_i(a'_i) = b'_i]$$

$$\left[[\mathsf{S}]^2_{(a,a'),(b,b')} = \mathbf{1}_{\operatorname{supp}(a\oplus a') = \operatorname{supp}(b\oplus b')} M^{-\ell} (M-1)^{-w(a\oplus a')} \right]$$



- Independent random functions
- input: $a = (a_1, ..., a_\ell)$
- output: $b = (b_1, ..., b_\ell)$
- $M = 2^m$



We obtain in a similar way that:

- Independent random functions
- input: $a = (a_1, ..., a_\ell)$
- output: $b = (b_1, ..., b_\ell)$
- $M = 2^m$

$$[\mathsf{F}]^2_{(a,a'),(b,b')} = \mathbf{1}_{\operatorname{supp}(b\oplus b')\subseteq \operatorname{supp}(a\oplus a')} M^{-\ell - w(a\oplus a')}$$

Properties of the two Decorrelation Modules



Introducing the two following transition matrices:

Properties of the two Decorrelation Modules

Introducing the two following transition matrices:

$$\mathsf{PS}_{(a,a'),\gamma} = \mathbf{1}_{\gamma = \mathrm{supp}(a \oplus a')}$$
$$\mathsf{SP}_{\gamma,(a,a')} = \mathbf{1}_{\gamma = \mathrm{supp}(a \oplus a')} M^{-\ell} (M-1)^{-w(\gamma)}$$

Properties of the two Decorrelation Modules

Introducing the two following transition matrices:

$$\mathsf{PS}_{(a,a'),\gamma} = \mathbf{1}_{\gamma = \mathrm{supp}(a \oplus a')}$$
$$\mathsf{SP}_{\gamma,(a,a')} = \mathbf{1}_{\gamma = \mathrm{supp}(a \oplus a')} M^{-\ell} (M-1)^{-w(\gamma)}$$

• SP × PS = Id and PS × SP = $[S]^2$ (similar result for $[F]^2$)

 \pm If M is a $2^{2m\ell} \times 2^{2m\ell}$ matrix such that there exists a $2^{\ell} \times 2^{\ell}$ matrix \overline{M} verifying

$$\mathsf{M}=\mathsf{PS}\times\overline{\mathsf{M}}\times\mathsf{SP}$$

then:

$$\|M\|_{\mathrm{a}} = |||M|||_{\infty} = |||\overline{M}|||_{\infty}$$

Part II: Designs and Security Proofs Dial C for Cipher

Description of C

C corresponds to the AES where "addRoundKeys \rightarrow SubBytes" is replaced by mutually independent random permutations.



Thomas Baignères

PhD Defense

Description of C

C corresponds to the AES where "addRoundKeys \rightarrow SubBytes" is replaced by mutually independent random permutations.



- C is made of 9 identical rounds, followed by a layer of substitution boxes.
- C uses 16 · 10 = 160 mutually independent random
 8-bits substitution boxes

More Notations...

- A plaintext of C is a 4x4 array of elements of GF(256)
- The support of a plaintext is the 4x4 array with 0's where the plaintext has 0's and 1's everywhere else.

0x2f 0x00 0xaa 0x90 0xc2 0x43 0x12 0x01 0x01 0x26 0x00 0x2f 0xf1 0x00 0x55 0x7b

plaintext
More Notations...

- A plaintext of C is a 4x4 array of elements of GF(256)
- The support of a plaintext is the 4x4 array with 0's where the plaintext has 0's and 1's everywhere else.



corresponding support

We consider a version of C reduced to 3 rounds:



Thomas Baignères

PhD Defense

We consider a version of C reduced to 3 rounds:



We consider a version of C reduced to 3 rounds:



PhD Defense

We consider a version of C reduced to 3 rounds:

We consider a version of C reduced to 3 rounds:



We consider a version of C reduced to 3 rounds:



We consider a version of C reduced to 3 rounds:



We consider a version of C reduced to 3 rounds:



For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times (\overline{\mathsf{L}})^{r-1} \times \mathsf{SP}$$

where \overline{L} is a square matrix indexed by supports (e.g. $2^{16} \times 2^{16}$)

For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times (\overline{\mathsf{L}})^{r-1} \times \mathsf{SP}$$

where $\overline{\mathsf{L}}$ is a square matrix indexed by supports (e.g. $2^{16}\times 2^{16})$

It is easy to show that $[C^*]^2$ can also be expressed in a similar way:

 $[\mathsf{C}^{\star}]^2 = \mathsf{PS} \times \overline{\mathsf{C}^{\star}} \times \mathsf{SP}$

For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times (\overline{\mathsf{L}})^{r-1} \times \mathsf{SP}$$

where $\overline{\mathsf{L}}$ is a square matrix indexed by supports (e.g. $2^{16}\times 2^{16})$

It is easy to show that $[C^*]^2$ can also be expressed in a similar way:

 $[\mathsf{C}^{\star}]^2 = \mathsf{PS} \times \overline{\mathsf{C}^{\star}} \times \mathsf{SP}$

$$[\mathbf{C}]^2 - [\mathbf{C}^{\star}]^2 = \mathsf{PS} \times \left((\overline{\mathsf{L}})^{r-1} - \overline{\mathsf{C}^{\star}} \right) \times \mathsf{SP}$$

For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times (\overline{\mathsf{L}})^{r-1} \times \mathsf{SP}$$

where $\overline{\mathsf{L}}$ is a square matrix indexed by supports (e.g. $2^{16}\times 2^{16})$

It is easy to show that $[C^*]^2$ can also be expressed in a similar way:

 $[\mathsf{C}^{\star}]^2 = \mathsf{PS} \times \overline{\mathsf{C}^{\star}} \times \mathsf{SP}$

$$[\mathbf{C}]^2 - [\mathbf{C}^{\star}]^2 = \mathsf{PS} \times \left((\overline{\mathsf{L}})^{r-1} - \overline{\mathsf{C}^{\star}} \right) \times \mathsf{SP}$$

$$\max_{\mathcal{A}} \operatorname{Adv}_{\mathcal{A}}(\mathbf{C}, \mathbf{C}^{\star}) = \frac{1}{2} |||(\overline{\mathsf{L}})^{r-1} - \overline{\mathsf{C}^{\star}}|||_{\infty}$$

For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times (\overline{\mathsf{L}})^{r-1} \times \mathsf{SP}$$

where $\overline{\mathsf{L}}$ is a square matrix indexed by supports (e.g. $2^{16}\times 2^{16})$

It is easy to show that $[C^*]^2$ can also be expressed in a similar way:

 $[\mathsf{C}^{\star}]^2 = \mathsf{PS} \times \overline{\mathsf{C}^{\star}} \times \mathsf{SP}$

$$[\mathbf{C}]^2 - [\mathbf{C}^{\star}]^2 = \mathsf{PS} \times \left((\overline{\mathsf{L}})^{r-1} - \overline{\mathsf{C}^{\star}} \right) \times \mathsf{SP}$$

$$\left(\max_{\mathcal{A}} \operatorname{Adv}_{\mathcal{A}}(\mathbf{C}, \mathsf{C}^{\star}) = \frac{1}{2} |||(\overline{\mathsf{L}})^{r-1} - \overline{\mathsf{C}^{\star}}|||_{\infty}\right)$$

Can we reduce the computational complexity even further?

Yes! But the diffusion has to be chosen with care...

The matrix \overline{L} can be expressed as

$$\overline{\mathsf{L}}_{\gamma,\gamma'} = 255^{-w(\gamma)} \mathrm{N}[\gamma,\gamma']$$

where $N[\gamma, \gamma']$ is the number of ways of connecting a support γ to a support γ' .

Control Using the fact that the MixColumns operation is a linear multipermutation, it can be shown that $N[\gamma, \gamma']$ only depends on

 \clubsuit the weights of the diagonals of γ

 \clubsuit the weights of the columns of γ'

 \blacksquare and thus it is also the case for \overline{L}















For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} imes \mathsf{SW} imes \left(\overline{\overline{\mathsf{L}}} imes \mathsf{W}\right)^{r-2} imes \overline{\overline{\mathsf{L}}} imes \mathsf{WS} imes \mathsf{SP}$$

where \overline{L} and W are a square matrices indexed by patterns of weights (e.g. 625×625)

For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times \mathsf{SW} \times \left(\overline{\overline{\mathsf{L}}} \times \mathsf{W}\right)^{r-2} \times \overline{\overline{\mathsf{L}}} \times \mathsf{WS} \times \mathsf{SP}$$

where \overline{L} and W are a square matrices indexed by patterns of weights (e.g. 625×625)

It is easy to show that $[C^*]^2$ can also be expressed in a similar way:

$$[\mathsf{C}^{\star}]^2 = \mathsf{PS} \times \mathsf{SW} \times \overline{\overline{\mathsf{C}^{\star}}} \times \mathsf{WS} \times \mathsf{SP}$$

For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times \mathsf{SW} \times \left(\overline{\overline{\mathsf{L}}} \times \mathsf{W}\right)^{r-2} \times \overline{\overline{\mathsf{L}}} \times \mathsf{WS} \times \mathsf{SP}$$

where \overline{L} and W are a square matrices indexed by patterns of weights (e.g. 625×625)

It is easy to show that $[C^*]^2$ can also be expressed in a similar way:

$$[\mathsf{C}^{\star}]^2 = \mathsf{PS} \times \mathsf{SW} \times \overline{\overline{\mathsf{C}^{\star}}} \times \mathsf{WS} \times \mathsf{SP}$$

$$[\mathbf{C}]^2 - [\mathbf{C}^*]^2 = \mathsf{PS} \times \mathsf{SW} \times \left(\left(\overline{\overline{\mathsf{L}}} \times \mathsf{W} \right)^{r-2} \times \overline{\overline{\mathsf{L}}} - \overline{\overline{\mathsf{C}^*}} \right) \times \mathsf{WS} \times \mathsf{SP}$$

For a *r*-round version of **C** we have:

$$[\mathbf{C}]^2 = \mathsf{PS} \times \mathsf{SW} \times \left(\overline{\overline{\mathsf{L}}} \times \mathsf{W}\right)^{r-2} \times \overline{\overline{\mathsf{L}}} \times \mathsf{WS} \times \mathsf{SP}$$

where \overline{L} and W are a square matrices indexed by patterns of weights (e.g. 625×625)

It is easy to show that $[C^*]^2$ can also be expressed in a similar way:

$$[\mathsf{C}^{\star}]^2 = \mathsf{PS} \times \mathsf{SW} \times \overline{\overline{\mathsf{C}^{\star}}} \times \mathsf{WS} \times \mathsf{SP}$$

$$[\mathbf{C}]^2 - [\mathbf{C}^{\star}]^2 = \mathsf{PS} \times \mathsf{SW} \times \left(\left(\overline{\overline{\mathsf{L}}} \times \mathsf{W} \right)^{r-2} \times \overline{\overline{\mathsf{L}}} - \overline{\overline{\mathsf{C}^{\star}}} \right) \times \mathsf{WS} \times \mathsf{SP}$$

$$\left(\max_{\mathcal{A}} \operatorname{Adv}_{\mathcal{A}}(\mathbf{C}, \mathsf{C}^{\star}) = \frac{1}{2} ||| \left(\overline{\overline{\mathsf{L}}} \times \mathsf{W}\right)^{r-2} \times \overline{\overline{\mathsf{L}}} - \overline{\overline{\mathsf{C}^{\star}}} |||_{\infty}\right)$$

Computing the advantage of the best distinguisher (either adaptive or not) only requires operations on 625×625 matrices (instead of $2^{256} \times 2^{256}$ initially).

Values of $\mathrm{Adv}_\mathcal{A}(C,C^\star)$

r	1	2	3	4	5	6
$\operatorname{Adv}(C, C^{\star})$	1	1	$2^{-4.0}$	$2^{-23.4}$	$2^{-45.8}$	$2^{-71.0}$
r	7	8	9	10	11	12
$\boxed{\operatorname{Adv}(C,C^{\star})}$	$2^{-126.3}$	$2^{-141.3}$	$2^{-163.1}$	$2^{-185.5}$	$2^{-210.8}$	$2^{-238.9}$

Values of $\mathrm{Adv}_\mathcal{A}(C,C^\star)$

r	1	2	3	4	5	6
$\operatorname{Adv}(C, C^{\star})$	1	1	$2^{-4.0}$	$2^{-23.4}$	$2^{-45.8}$	$2^{-71.0}$
r	7	8	9	10	11	12
$\operatorname{Adv}(C, C^{\star})$	$2^{-126.3}$	$2^{-141.3}$	$2^{-163.1}$	$2^{-185.5}$	$2^{-210.8}$	$2^{-238.9}$

7 rounds of C are enough to obtain provable security against 2-limited adversaries

Other Security Results

Using decorrelation techniques, the security results concerning 2-limited adversaries immediately imply security bounds against:

- linear and differential cryptanalysis (the linear hull and the differentials effect being taken into account)
- iterated attacks of order 1

After some more computations, we manage to compute the exact security against LC and DC, prove that no impossible differential exists, and show that C tends towards the perfect cipher as r increases (as far as LC and DC are concerned).

Part II: Designs and Security Proofs KFC: the Krazy Feistel Cipher We did not manage to prove the security of C against higher *q*-limited adversaries for q > 2.

We did not manage to prove the security of C against higher *q*-limited adversaries for q > 2.

Idea: try to bound the advantage of the best q-limited adversary by that of the best (q-1)-limited adversary.



Rand. Permutations vs. Rand. Functions





 Non negligible risk of collision after a F-box



- Non negligible risk of collision after a F-box
- Use the "sandwich technique" to obtain (almost) pairwise independent inputs before the layer of random functions.



- Non negligible risk of collision after a F-box
- Use the "sandwich technique" to obtain (almost) pairwise independent inputs before the layer of random functions.
- The construction is not invertible. We plug it in a Feistel scheme.



- With this approach, we manage to prove the security against adversaries up to the order 70 (for an unreasonable set of parameters).
- The bounds are not tight at all it is certainly possible to improve our results.
- With this approach, we manage to prove the security against adversaries up to the order 70 (for an unreasonable set of parameters).
- The bounds are not tight at all it is certainly possible to improve our results.

Part II: Designs and Security Proofs Critics

Requirements & Uncovered Attacks

- C might never fit, say, RFID tags (in the best case, we need 160kB of memory to store the tables).
- We proposed so-called "provably secure" block ciphers...
- ...which are not provably secure against all known attacks.
- e.g., C is not provably secure against cache attacks or saturation attacks.

On the Independence of the Round Keys

- Our proofs assume that the round are mutually independent.
- This is not true in practice: thousands of bits of randomness are derived from a 128 bit key.
- Using a cryptographically secure PRNG, we can show that if an attack applies on the block cipher with the key schedule, but not on the block cipher with mutually independent rounds, then the PRNG's sequence can be distinguished from pure random.

Two Sides to Every Story

- Pessimistic view (not my favorite):
 - Since we need more bits of randomness to generate the boxes than the number of bits we are allowed to encrypt, why not use the bits generated with BBS or QUAD as a one-time-pad... and throw away all the constructions? 3
- Optimistic View:
 - The assumption about the independence of the round keys has nothing to do with the block cipher itself, but with the key schedule.
 - If a "provably secure" block cipher is broken by an attack against which it should resist make the key schedule stronger!
 - Making sure that the distribution matrix of the block cipher considered is close to that of C* appears to be very natural. Independently of the key schedule, it's a strong security argument.

Conclusion

"[...] the methodology of provable security has become unavoidable in designing and evaluating new schemes" [JSe03] "[...] the methodology of provable security has become unavoidable in designing and evaluating new schemes" [JSe03]

public key schemes

 \square

"[...] the methodology of provable security has become unavoidable in designing and evaluating new schemes" [JSe03]

public key schemes

We hope to have made a significant step towards its extension to block ciphers!

Thank you for your attention!

Publications

[BVicits08] The Complexity of Distinguishing Distributions Joint work with Serge Vaudenay Published in the proceedings of ICITS 08 (Calgary, Canada)

[BSVsac07] Linear Cryptanalysis of Non Binary Ciphers (with an application to SAFER) Joint work with Jacques Stern & Serge Vaudenay Published in the proceedings of SAC 07 (Ottawa, Canada)

[BFa06] KFC - *The Krazy Feistel Cipher* Joint work with Matthieu Finiasz Published in the proceedings of Asiacrypt 06 (Shangai, China)

[BFsac06] *Dial C for Cipher* Joint work with Matthieu Finiasz Published in the proceedings of SAC 06 (Montreal, Canada)

[BVsac05] Proving the Security of the AES Substitution-Permutation Network Joint work with Serge Vaudenay Published in the proceedings of SAC 05 (Kingston, Canada)

[BJVa04] How Far Can We Go Beyond Linear Cryptanalysis? Joint work with Pascal Junod & Serge Vaudenay Published in the proceedings of Asiacrypt 04 (Jeju Island, Korea)